Mass of Jupiter
Pre-Lab Quiz

Record your team’s answers as well as your reasonings and explanations.

1. 

2. 

3. 

4. 
Part 1: Identifying the Galilean Moons

Using the MACRO Professor Robert L. Mutel Telescope (RLMT), Jupiter has been imaged five times over two days (note the timestamps in the lower right of the images in the figure below).
1. In the images provided, as time passes, why do the Galilean moons appear to move along a line from upper left of the images to bottom right of the images? (Why don’t the moons orbit around Jupiter in a circle (ellipse) as if you're viewing everything from above?)

2. Using Stellarium or the Find Jupiter's Moons App linked on the lab webpage for this part of the lab, identify each of the four Galilean moons shown in Images 3 and 5. For each image, you can either label the moons on the figure on the previous page or list the names of the moons below in order of appearance from left to right.

   Note: The RLMT is located near Tucson, AZ, which is on Mountain Time and in early November 2020 was at UT-6 hours.

3. In Image 1, why do you think the fourth Galilean moon, Callisto, is not labeled or pictured?
4. Between the times Image 1 and Image 4 were taken, Jupiter’s moon Io completed exactly one full orbit around Jupiter. What is $P$, the orbital period of Io, the time it takes to go around Jupiter once, in hours, days, and Earth years?

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5. As Io was imaged as it orbited Jupiter, the imaging time of Image 4 was noteworthy. This is because at this time, Io was at the furthest right of Jupiter of any other time in its orbit. Because of this, Image 4 can be used to identify $a$, Io’s semi-major axis, or Io’s average distance from Jupiter. We will use $\theta$ for $a$ in arcseconds and $D$ for $a$ in astronomical units (AU, or the average Earth to Sun distance) to be consistent with the version of the Small Angle Formula we’ve worked with before. In Image 4 above, $\theta$ is given in pixels. Noting that the pixel scale of the RLMT is 0.54”/pix, what is $\theta$ in arcseconds?
Part 2: Applying Kepler’s Law

1. Use Stellarium or the Find Jupiter’s Moons App linked on the lab webpage for this part of the lab to find the value of $d$, the distance from Earth to Jupiter at the time of your images in AU at the time these images were taken. Record $d$ below.

2. Using the Small Angle Formula below, $d$ in AU from Question 1, and $\theta$ in arcseconds from Question 5 in Part 1, determine Io’s semi-major axis $D$ in AU, rearranging the Small Angle Formula as needed.

$$\theta_{\text{arcseconds}} = 206265 \times \frac{D_{\text{AU}}}{d}$$
3. Using semimajor axis $D$ in AU from Question 2, $P$ in Earth years from Question 4 in the previous part of this lab, and the version of Kepler’s Third Law below, determine the mass of Jupiter $M$ in solar masses, $M_{\text{Sun}}$.

Note: In order for this version of Kepler’s Third Law to apply, where $M$ is returned in $M_{\text{Sun}}$, $D$ must be in AU and $P$ must be in Earth years.

$$M = \frac{D^3}{P^2}$$

4. What is the mass of Jupiter $M$, not relative to the Sun in solar masses, $M_{\text{Sun}}$, as before, but relative to the Earth in Earth masses, $M_{\text{Earth}}$?

Note: $332,900 M_{\text{Earth}} = 1 M_{\text{Sun}}$. 